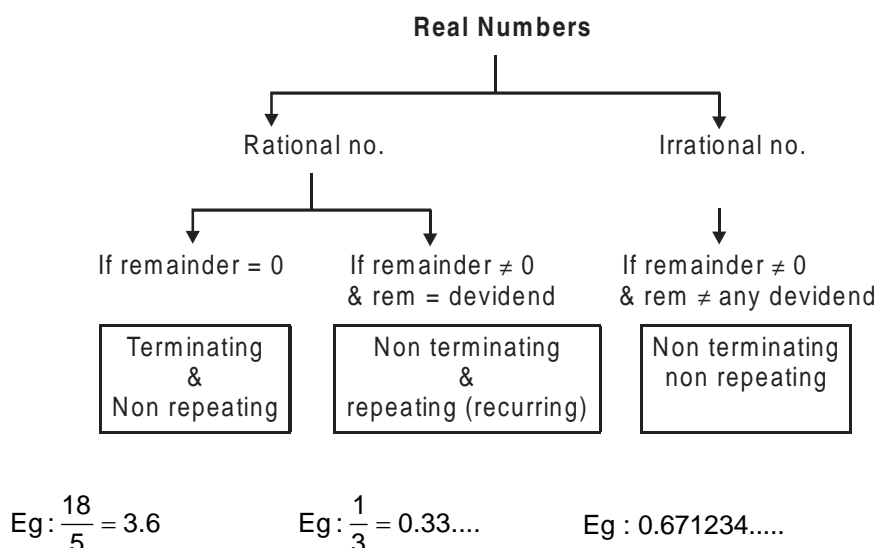


# 1

## Real Number

### Fundamentals:



- If  $a$  is a real number, modulus  $a$  is written as  $|a|$ ;  $|a|$  is always positive or zero.
- All natural number which cannot be divided by any number other than 1 and itself is called a prime number.
- A non-negative integer ' $p$ ' is said to be divided by an integer ' $q$ ' if there exists an integer ' $d$ ' such that:  

$$p = qd$$
- $\pm 1$  divides every non-zero integer.
- 0 does not divide any integer.

**Euclid's Division Lemma:** Let  $a$  and  $b$  be any two positive integers, then there exists unique integers  $q$  and  $r$  such that:  $a = bq + r$ ,  $0 \leq r < b$

**Euclid's Division Algorithm:** Let  $a$  and  $b$  be any two positive integers such that  $a > b$  and ' $q$ ' and ' $r$ ' as quotient and remainder

Take  $a$  as dividend and  $b$  as divisor  $a = bq + r$ ,  $0 < r < b$

Then every common divisor of  $a$  and  $b$  is a common divisor of  $b$  and  $r$ .

- Finding HCF of two positive integers using Euclid's Division Algorithm:

**Step 1:** Apply Euclid's lemma to  $a$  and  $b$ :  $a = bq_1 + r_1$

**Step 2:** If  $r_1 = 0$ , then  $HCF = b$ .

**Step 3:** If  $r_1 \neq 0$ , then again apply Euclid's lemma:  $b = q_1r_1 + r_2$

**Step 4:** If  $r_2 = 0$ , then  $HCF = r_1$ .

**Step 5:** If  $r_2 \neq 0$ , then again apply Euclid's lemma till remainder  $r_n = 0$ , then the divisor is  $HCF$ .

### Fundamental Theorem of Arithmetic:

Every composite number can be expressed as a product of primes, and this factorisation is unique except for the order in which the prime factors occur.

Important Theorems:

1. Let  $p$  be a prime number and  $a$  be a positive integer. If  $p$  divides  $a^2$ , then  $p$  divides  $a$ .
2. Consider two positive integers  $a$  and  $b$ , then  $LCM \times HCF = a \times b$ .

3. Let  $x$  be a rational number whose decimal expansion terminates. Then we can express  $x$  in the form  $\frac{p}{q}$ , where  $p$  and  $q$  are co-prime and the prime factorisation of  $q$  is of the form  $2^n 5^m$ , where  $n, m$  are non-negative integers.
4. Let  $x = \frac{p}{q}$  be a rational number, such that the prime factorisation of  $q$  is of the form  $2^n 5^m$ , where  $n, m$  are non-negative integers. Then  $x$  has a decimal expansion which terminates.
5. Let  $x = \frac{p}{q}$  be a rational number, such that the prime factorisation of  $q$  is not of the form  $2^n 5^m$ , where  $n, m$  are non-negative integers. Then  $x$  has a decimal expansion which is non-terminating repeating.